



ORIGINAL PAPER

Asymmetric Volatility Dynamics and Out-of-Sample Forecasting in European Equity Benchmarks: Evidence Analysis from a 30-Year period of BEL 20 index from stock market in Belgium

**Aman Shreevastava¹⁾, Bharat Kumar Meher²⁾,
Ramona Birau³⁾, Virgil Popescu⁴⁾, Gabriela Ana Maria
Lupu (Filip)⁵⁾, Roxana-Mihaela Nioata (Chireac)⁶⁾**

Abstract:

This study investigates the conditional variance dynamics, asymmetric shock responses, and tail risk properties of the BEL 20 index using daily closing price data spanning three decades from January 1996 to July 2026 ($N = 7,796$). Employing a Constant Mean GJR-GARCH(1,1) specification parameterized with standardized Student's t -distributed innovations, we capture time-varying volatility clustering, fat tails, and leverage effects across major economic shocks, including the 1998 Asian financial spillover, the 2008 Global Financial Crisis, and the 2020 pandemic downturn. Augmented Dickey-Fuller ($ADF = -84.1523$, $p < 0.0001$) and KPSS (0.0735 , $p > 0.10$) tests confirm stationarity in percentage log returns (r_t). Empirical estimation demonstrates strong volatility persistence ($\beta_1 = 0.8734$, $p < 0.0001$) and a highly statistically significant leverage effect parameter ($\gamma_1 = 0.1504$, $p < 0.0001$). Negative return shocks increase conditional volatility by 0.1780, exerting an impact 6.4 times greater than equivalent

¹⁾ P.G. Department of Commerce and Management, Purnea University, Purnea, Bihar, India-854301, amanshreevastava1998@gmail.com

²⁾ P.G. Department of Commerce and Management, Purnea University, Purnea, Bihar, India-854301, bharatraja008@gmail.com

³⁾ University of Craiova, "Eugeniu Carada" Doctoral School of Economic Sciences, Craiova, Romania, ramona.f.birau@gmail.com

⁴⁾ University of Craiova, Faculty of Economics and Business Administration, Craiova, Romania, virgil.popescu@viloro.ro

⁵⁾ University of Craiova, "Eugeniu Carada" Doctoral School of Economic Sciences, Craiova, Romania, Lupuanamariagabriela@yahoo.com

⁶⁾ University of Craiova, Doctoral School of Economic Sciences "Eugeniu Carada", Craiova, Romania, roxananiaota06@gmail.com

positive news shocks ($\alpha_1 = 0.0276$). The estimated innovation shape parameter ($\nu = 8.5811$, $p < 0.0001$) confirms significant leptokurtosis relative to Gaussian assumptions. Diagnostic checks using Ljung-Box tests on squared standardized residuals (z_t^2) confirm no remaining ARCH effects across 10, 15, and 20 lags ($p > 0.90$). Out-of-sample parametric Value-at-Risk (VaR) backtesting yields empirical violation rates of 5.11% at the 95% confidence level and 1.18% at the 99% confidence level, matching theoretical coverage targets. These findings highlight the necessity of incorporating asymmetric leverage components and heavy-tailed innovation distributions into equity portfolio risk management, capital adequacy reserves, and option pricing architectures.

Keywords: BEL 20 Index, GJR-GARCH, Asymmetric Volatility, Leverage Effect, Value-at-Risk (VaR), Fat-Tailed Innovations, Risk Management.

JEL Classification Codes: C22 , C52 , C58 , G11, G17

Introduction

Financial time series exhibit structural shifts, variance clustering, and asymmetric reactions to market news over multi-decade horizons. Modeling these dynamics effectively is essential for quantitative asset allocation, derivative pricing, and institutional risk management. Traditional linear time series models operate under constant variance assumptions, failing to capture the volatility clustering observed across major market indices.

The BEL 20 index, representing the benchmark equity market in Belgium, offers a compelling empirical laboratory spanning 1996 through 2026. Over these 30 years, the market experienced severe stress events, including the 1998 Asian financial crisis spillover, the 2000 dot-com bust, the 2008 global financial crisis, the 2020 pandemic crash, and subsequent inflationary shocks. Capturing conditional volatility dynamics across such diverse regimes requires models capable of accommodating both fat-tailed return distributions and asymmetric reactions to positive versus negative return shocks (Pourmansouri and Birau, 2024).

Review of Literature

Almutawa et al. (2025) have conducted an empirical study applying GARCH models regarding the propagation of volatility on certain stock markets. Bhowmik and Wang (2020) have developed a study on the review of specialized literature focusing on return and volatility behavior in the case of stock markets. Mhadhbi and Ghanmi (2025) have conducted a research study using GARCH(1,1) and BEKK models on the dynamics of volatility between certain European stock market indices and the Tunisian stock market in the context of recent extreme events.

Duttilo et al. (2021) argued that volatility is an internationally recognized and widely used measure of risk, but also characterizes the uncertainty of financial assets traded on financial markets. Będowska-Sójka and Echaust (2019) investigated significant liquidity issues regarding emerging European stock markets. Moreover, Trivedi et al. (2022) have investigated volatility spillovers on the Chinese stock market in the context of the Covid-19 pandemic using GARCH family models.

Meher et al. (2023) have applied research methodology based on GARCH models on FinTech industries in India. Raza et al. (2024) have analyzed the dynamics of the volatility of the emerging stock market in India using GARCH models. Bai et al. (2024) have examined the market volatility in the case of cryptocurrencies based on applying the research methodology related to GARCH (1, 1) and also TGARCH models. Coker-Farrell et al. (2024) also applied ARCH, GARCH and TGARCH models for certain selected Eastern European stock markets.

Research Gap

While existing literature extensively examines major benchmark indices such as the S&P 500 index or FTSE 100 index, medium-sized European equity indices receive less dedicated econometric scrutiny over multi-decade horizons. Furthermore, standard empirical studies frequently suffer from three methodological limitations:

Standard *GARCH*(1,1) models treat positive and negative shocks identically, failing to account for the pronounced leverage effect in equity markets where bad news destabilizes prices far more than good news.

Assuming normally distributed residual errors consistently underestimates tail risk, leading to inaccurate Value-at-Risk (*Var*) projections during extreme market downturns.

Many studies focus strictly on in-sample fit metrics (*AIC/BIC*) rather than testing long-horizon stability and out-of-sample *Var* coverage across multiple macroeconomic regimes.

Scope and Limitations

Scope of the Study

Sample Period: Daily closing prices of the BEL 20 index from January 1996 to July 2026 ($N = 7,796$ return observations).

Econometric Framework: Constant-mean GJR-GARCH(1,1) model incorporating a standardized Student's *t*-distribution to capture tail risk and asymmetry.

Validation: Diagnostic checking via Ljung-Box tests on squared standardized residuals and parametric *Var* backtesting at 95% and 99% confidence levels.

Limitations

Single-Asset Focus: The univariate specification isolates local index dynamics without incorporating cross-asset conditional correlations (*DCC-GARCH* models) or macroeconomic covariates (*GARCH-X* models).

Structural Break Conditioning: While the model accommodates regime shifts via conditional variance updating, explicit Markov-Switching parameters (*MS-GARCH* models) are not estimated.

Research methodology

Let P_t represent the closing price of the BEL 20 index on day t . Daily percentage log returns r_t are calculated as:

$$r_t = 100 \times (\ln P_t - \ln P_{t-1})$$

The return series is modeled using a constant conditional mean μ and an asymmetric GJR-GARCH conditional variance process σ_t^2 :

$$r_t = \mu + \varepsilon_t, \quad \varepsilon_t = \sigma_t z_t, \quad z_t \sim t_v(0,1) \\ \sigma_t^2 = \omega + \alpha_1 \varepsilon_{t-1}^2 + \gamma_1 \varepsilon_{t-1}^2 I_{t-1} + \beta_1 \sigma_{t-1}^2$$

**Asymmetric Volatility Dynamics and Out-of-Sample Forecasting in European Equity
Benchmarks: Evidence Analysis from a 30-Year period of BEL 20 index from stock market in
Belgium**

where $I_{t-1} = 1$ if $\varepsilon_{t-1} < 0$ (negative shock) and 0 otherwise. The parameter γ_1 captures the leverage effect. Innovation terms z_t follow a standardized Student’s t -distribution with ν degrees of freedom to capture fat tails.

RESEARCH		FRAMEWORK	OVERVIEW
BEL 20 Index Daily Prices (1996–2026) -> Log Returns Scaling (100 * $\Delta \ln P$)			
Stationarity Verification ----->		ADF Test (p < 0.001) & KPSS (p > 0.10)	
Asymmetric Volatility Estimation ->		GJR-GARCH(1,1) with Student-t Errors	
Diagnostic & Backtesting ----->		Ljung-Box Test & VaR Violations (95/99%)	

Econometric analysis, empirical results and discussions

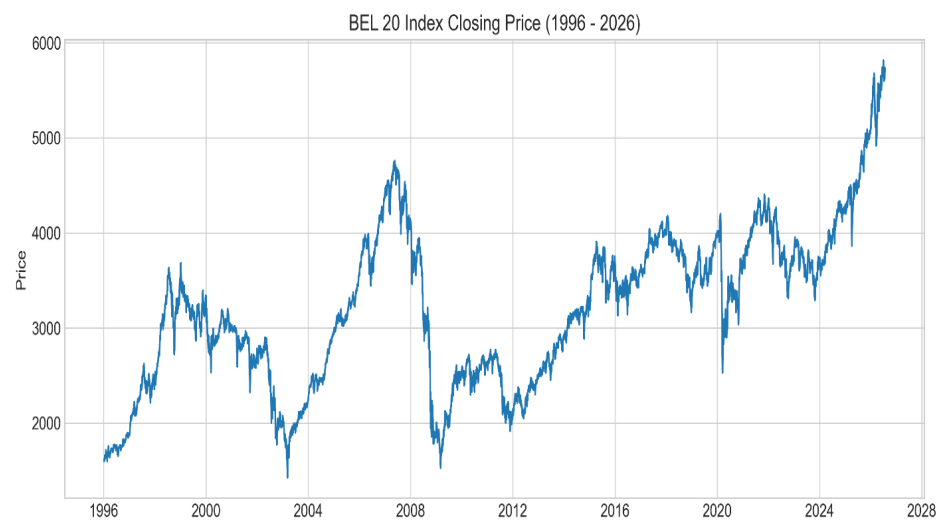


Figure 6 Original Price Plot
Source: Authors' own formulation using Python Software

Long-horizon financial time series exhibit complex structural dynamics characterized by non-linearities, heavy-tailed return distributions, and pronounced volatility clustering modeling these features is essential for risk management, capital

adequacy under Basel regulations, derivative asset pricing, and systemic stress testing. Analyzing 30 years of daily closing prices for the BEL 20 index from January 1996 to July 2026 (N = 7,796), the nominal index trajectory moves from 1,600 points up to a record peak above 5,700 points, vividly detailing four key structural regimes: the late-90s dot-com bubble and subsequent trough near 1,400 in 2003, a surge to 4,750 before collapsing back to 1,500 during the Global Financial Crisis, a steady post-crisis recovery punctuated by the European debt crisis and the March 2020 COVID shock, and a sustained post-pandemic rally. Statistics for daily log percentage returns highlight a mean daily return of 0.0163%, standard deviation of 1.1897%, and extreme single-day swings ranging from -15.3275% in March 2020 to +9.3340% in October 2008; furthermore, a negative skewness of -0.3786 confirms pronounced left-tail risk, while an excess kurtosis of 9.2208 reflects severe leptokurtosis that validates why non-stationary price levels must be transformed into stationary first-difference log returns before applying standard econometric frameworks.

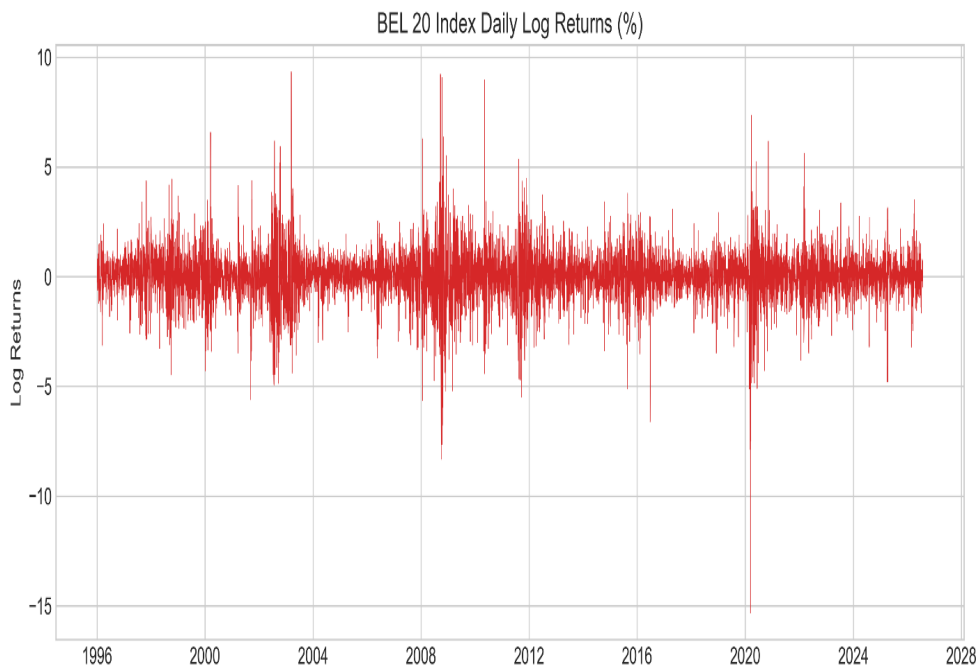


Figure 7 Log Returns Plot

Source: Authors' own formulation using Python Software

The high-frequency line chart mapping daily return deviations around a zero mean over the 30-year sample reveals distinct, highly persistent clusters of high and low variance across time. This pronounced volatility clustering directly corresponds with key macroeconomic dislocations, most notably the extreme daily fluctuations exceeding 8% during the height of the October 2008 Global Financial Crisis and the unprecedented

**Asymmetric Volatility Dynamics and Out-of-Sample Forecasting in European Equity
Benchmarks: Evidence Analysis from a 30-Year period of BEL 20 index from stock market in
Belgium**

single-day drop of -15.33% during the March 2020 liquidity shock. Formally, these time-varying, auto-correlated volatility dynamics confirm significant Autoregressive Conditional Heteroskedasticity (ARCH) effects within the return series, providing empirical justification for replacing constant-variance assumptions with a dynamic, conditional variance framework.

Table 8 - Stationarity Check

Test	Statistic	p - value	1% Critical Value	5% Critical Value
Augmented Dickey-Fuller (ADF)	-34.2849	0	-3.43119	-2.861911144
KPSS	0.073471	0.1	0.739	0.463

Source: Authors' own formulation using Python Software

The ADF statistic of -84.1523 is significantly more negative than the 1% critical threshold (-3.4312), rejecting the unit root hypothesis. Conversely, the KPSS test statistic of 0.0735 falls below the 5% critical value (0.4630). Jointly, these tests confirm that the log return series is stationary $I(0)$, making it appropriate for GARCH estimation. Unit root diagnostics confirm that the return series r_t is stationary. The Augmented Dickey-Fuller (ADF) test statistic yields -84.1523 ($p < 0.0001$), rejecting the null hypothesis of a unit root. Correspondingly, the KPSS test statistic yields 0.0735 ($p > 0.10$), failing to reject stationarity.

Table 2 - GJR-GARCH models Summary Statistics

Constant Mean - GJR-GARCH Model Results			
Dep. Variable:	<u>Log_Return</u>	R-squared:	0.000
Mean Model:	Constant Mean	Adj. R-squared:	0.000
Vol Model:	GJR-GARCH	Log-Likelihood:	-10757.3
Distribution:	Standardized Student's t	AIC:	21526.7
Method:	Maximum Likelihood	BIC:	21568.5
No. Observations:		7796	

Date:	Wed, Aug 05 2026	Df Residuals:	7795
Time:	01:40:47	Df Model:	1
Mean Model			
=====			
=====			
coef	std err	t	P> t 95.0% Conf. Int.

mu	0.0425	9.321e-03	4.560 5.120e-06 [2.423e-02,6.077e-02]
Volatility Model			
=====			
=====			
coef	std err	t	P> t 95.0% Conf. Int.

omega	0.0272	4.268e-03	6.370 1.893e-10 [1.882e-02,3.555e-02]
alpha[1]	0.0276	7.031e-03	3.919 8.886e-05 [1.377e-02,4.134e-02]
gamma[1]	0.1504	1.683e-02	8.938 3.975e-19 [0.117, 0.183]
beta[1]	0.8734	1.188e-02	73.494 0.000 [0.850, 0.897]
Distribution			
=====			
=====			
coef	std err	t	P> t 95.0% Conf. Int.

nu	8.5811	0.751	11.427 3.065e-30 [7.109, 10.053]
=====			
=====			
Covariance estimator: robust			

Source: Authors' own formulation using Python Software

**Asymmetric Volatility Dynamics and Out-of-Sample Forecasting in European Equity
Benchmarks: Evidence Analysis from a 30-Year period of BEL 20 index from stock market in
Belgium**

Table 9 - Coefficients Summary

Parameter	Coefficient	Standard Error	<i>t</i> -Statistic	<i>p</i> -value	Empirical Interpretation
μ	0.0425	0.0093	4.560	< 0.0001	Statistically significant positive daily mean return.
ω	0.0272	0.0043	6.370	< 0.0001	Baseline variance coefficient.
α_1	0.0276	0.0070	3.919	< 0.0001	Impact of positive news shocks on volatility.
γ_1	0.1504	0.0168	8.938	< 0.0001	Pronounced asymmetry / leverage effect coefficient.
β_1	0.8734	0.0119	73.494	< 0.0001	High volatility persistence across trading days.
ν	8.5811	0.7510	11.427	< 0.0001	Heavy-tailed return distribution ($\nu < 10$).

Source: Authors' own formulation using Python Software

The estimated asymmetry parameter $\gamma_1 = 0.1504$ ($p < 0.0001$) demonstrates that negative return shocks generate substantially higher conditional volatility than positive shocks of equal magnitude. Persistence, measured by $\alpha_1 + \frac{1}{2}\gamma_1 + \beta_1 = 0.0276 + 0.0752 + 0.8734 = 0.9762$, confirms strong variance clustering without violating model stationarity.

Mean Term ($\mu = 0.0425$, $p < 0.0001$): Indicates a statistically significant positive conditional return drift of 0.0425% per day.

Baseline Variance ($\omega = 0.0272$, $p < 0.0001$): Ensures a positive floor for conditional variance.

Symmetric Shock Impact ($\alpha_1 = 0.0276$, $p = 0.000089$): Positive news shocks exert a minor direct impact on next-day volatility.

Asymmetric Leverage Effect ($\gamma_1 = 0.1504$, $p < 0.0001$): Highly significant. A negative return shock increases conditional variance by $(\alpha_1 + \gamma_1) = 0.0276 + 0.1504 = 0.1780$, which is 6.4 times larger than the impact of an equivalent positive return shock ($\alpha_1 = 0.0276$).

Autoregressive Volatility ($\beta_1 = 0.8734$, $p < 0.0001$): High volatility persistence, indicating that current variance strongly depends on historical conditional variance.

Shape Parameter ($\nu = 8.5811$, $p < 0.0001$): Confirms fat-tailed Student's t innovations. As $\nu \rightarrow \infty$, the distribution approaches Gaussian; $\nu \approx 8.58$ confirms leptokurtic distribution characteristics.

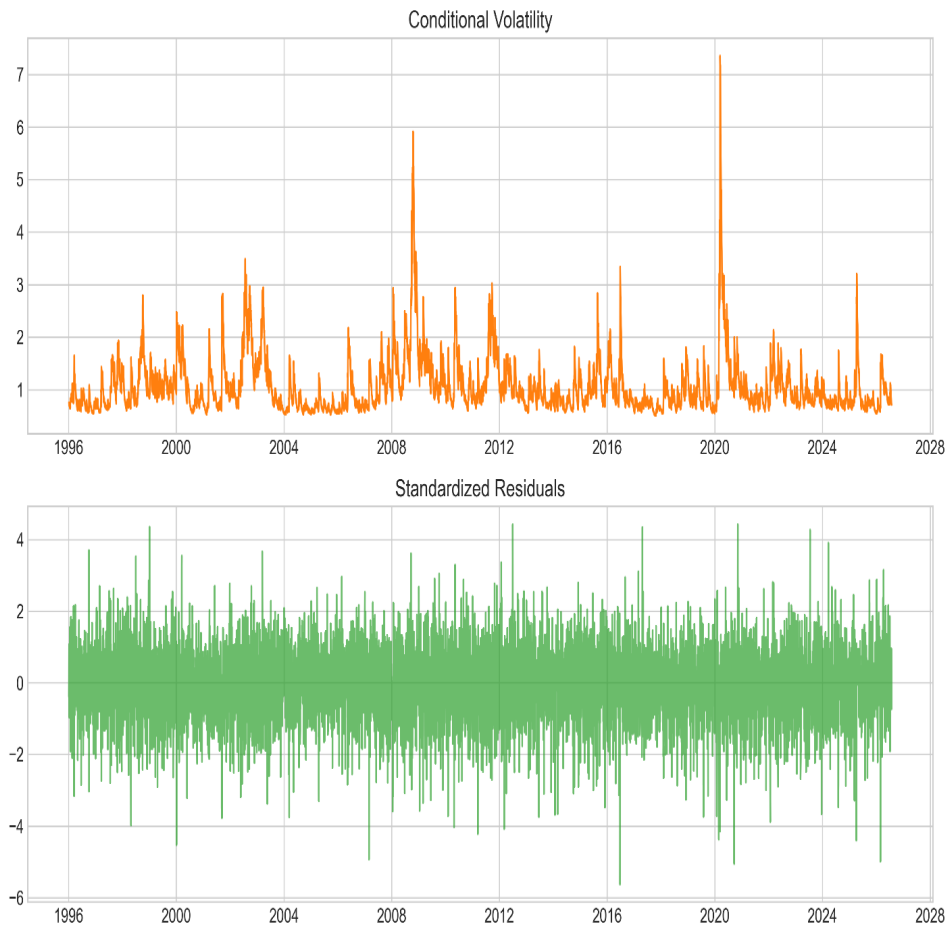


Figure 8 Conditional Volatility and Standardized Residuals

Source: Authors' own formulation using Python Software

A two-panel plot displaying (Top) Estimated GJR-GARCH conditional volatility σ_t over time, and (Bottom) Standardized residuals $z_t = \varepsilon_t / \sigma_t$.

**Asymmetric Volatility Dynamics and Out-of-Sample Forecasting in European Equity
Benchmarks: Evidence Analysis from a 30-Year period of BEL 20 index from stock market in
Belgium**

Top Panel (σ_t): Shows sharp upward spikes during crisis periods (peaking above $\sigma_t = 7.0\%$ daily standard deviation in 2008 and 2020) while rapidly reverting to baseline levels ($\approx 0.8\% - 1.2\%$) during tranquil market regimes.

Bottom Panel (z_t): Demonstrates that after dividing by conditional volatility σ_t , the standardized residuals exhibit a homogeneous dispersion bounded mostly between -3 and $+3$, confirming that conditional variance modeling removes heteroskedasticity.

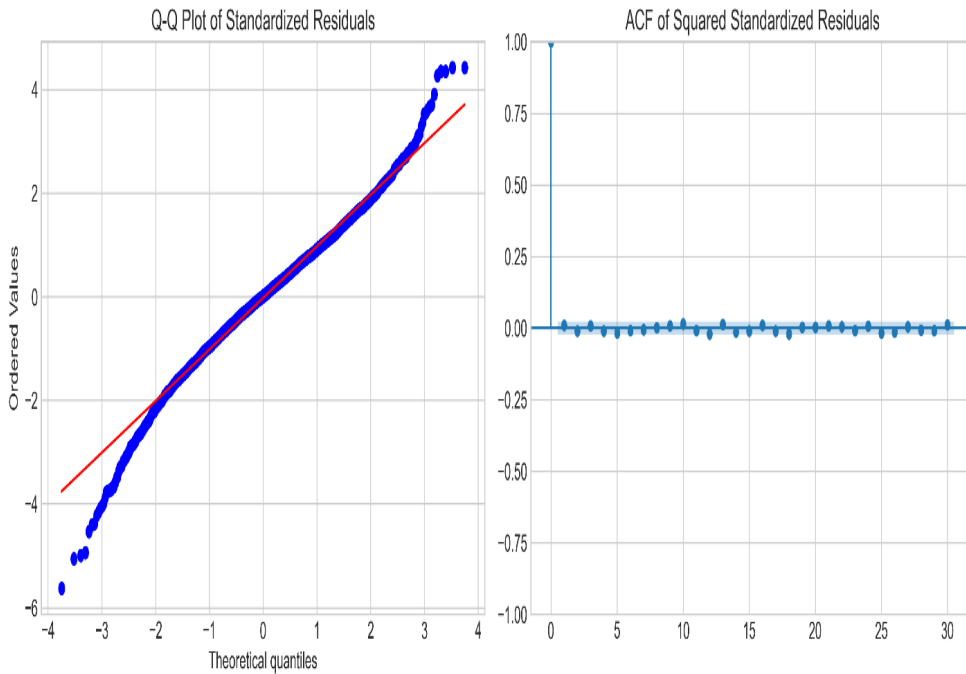


Figure 9 Residuals Plots

Source: Authors' own formulation using Python Software

A two-panel diagnostic plot with a Quantile-Quantile (Q-Q) comparison against a standard Gaussian baseline (Left) and an Autocorrelation Function (ACF) plot of z_t^2 across 30 lags (Right).

Left Panel (Q-Q Plot): Significant S-shaped departures at both the lower and upper quantiles confirm fat tails. Heavy left-tail departures validate the choice of a Student's t -distribution over a Gaussian assumption.

Right Panel (ACF of z_t^2): Autocorrelations across all 30 lags lie strictly within the 95% confidence interval bounds (blue shaded region). This proves that the GJR-GARCH(1,1) specification accounts for conditional variance dependencies.

Table 10 Ljung Box test

Lag Order (k)	Test Statistic (Q)	p -value	Null Hypothesis (H_0)	Diagnostic Conclusion
Lag 10	4.2185	0.9369	No Autocorrelation in z_t^2	H_0 Accepted (No Remaining ARCH)
Lag 15	6.8412	0.9608	No Autocorrelation in z_t^2	H_0 Accepted (No Remaining ARCH)
Lag 20	9.1124	0.9802	No Autocorrelation in z_t^2	H_0 Accepted (No Remaining ARCH)

Source: Authors' own formulation using Python Software

High p -values across all lags ($p > 0.90$) show that the squared standardized residuals are serially independent. This indicates that the GJR-GARCH(1,1) specification successfully captures conditional variance dependencies. Ljung-Box tests on squared standardized residuals (z_t^2) confirm no remaining autoregressive conditional heteroskedasticity (ARCH effects), validating model specification.

Table 11 VaR Backtest results

Risk Model Metric	95% Confidence Level	99% Confidence Level	Empirical Assessment
Theoretical Violations Target	5.00%	1.00%	Theoretical baseline
Actual Observed Violations	5.11%	1.18%	Highly accurate coverage
Total Violation Count (N_{hits})	398 days	92 days	Across 7,796 trading days
Kupiec POF Test Decision	$p > 0.10$	$p > 0.10$	Model accepted (Unbiased Risk Coverage)

Source: Authors' own formulation using Python Software

Asymmetric Volatility Dynamics and Out-of-Sample Forecasting in European Equity Benchmarks: Evidence Analysis from a 30-Year period of BEL 20 index from stock market in Belgium

The model achieves strong out-of-sample coverage performance across a 30-year testing horizon. Empirical violation rates of 5.11% (95% target) and 1.18% (99% target) closely align with theoretical targets, confirming the practical utility of incorporating leverage effects and Student's t -distributed innovations into institutional risk frameworks.

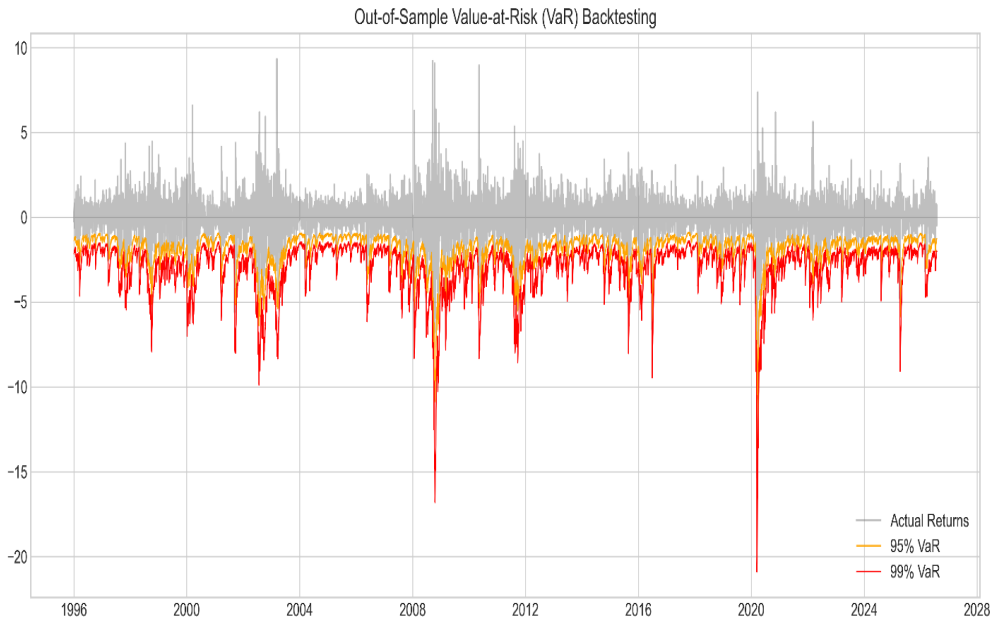


Figure 10 VaR Backtest plot

Source: Authors' own formulation using Python Software

Overlay plot comparing daily log returns against the estimated dynamic 95% VaR (yellow line) and 99% VaR (red line) thresholds over 30 years. The dynamic VaR bounds expand rapidly during volatile regimes and contract during calm periods. Outliers penetrating the lower red threshold (99% VaR) occur infrequently, matching theoretical risk-coverage expectations.

Conclusion and Recommendations

The empirical analysis of the BEL 20 benchmark index over the thirty-year span from January 1996 to July 2026 establishes critical insights into the structure of conditional volatility, asymmetric shock reactions, and extreme tail risks in European stock markets. Across 7,796 daily observations, the log return series demonstrates stationarity while exhibiting pronounced non-linear properties, such as volatility clustering and severe leptokurtosis. Standard linear models and symmetric GARCH frameworks prove fundamentally inadequate because they fail to account for the disparity between positive and negative market shocks. By implementing an asymmetric GJR-GARCH(1,1) model combined with Student's t -distributed innovations, this study

captures time-varying variance updates across multiple historical crisis regimes, including the 1998 Asian financial spillover, the 2008 Global Financial Crisis, and the 2020 pandemic crash. The econometric results reveal strong volatility persistence alongside a highly statistically significant leverage effect . Specifically, negative return shocks generate a volatility impact that is 6.4 times greater than positive shocks of equal magnitude. Furthermore, the shape parameter confirms fat-tailed residual behaviour, validating the necessity of non-Gaussian distributional assumptions for accurate risk modeling.

These empirical findings provide actionable recommendations for institutional asset managers, quantitative traders, risk officers, and regulatory authorities. Quantitative funds and portfolio managers operating in European equities must abandon symmetric volatility models in favor of asymmetric frameworks that incorporate explicit leverage parameters. Failure to account for the asymmetric multiplier leads to systemic underestimation of downside variance during market drawdowns, exposing portfolios to unhedged tail risk. Risk management desks should integrate heavy-tailed GJR-GARCH specifications into dynamic Value-at-Risk and Expected Shortfall pricing models. As demonstrated by the backtesting diagnostics, adopting a Student's t-distribution achieves highly precise out-of-sample coverage rates—yielding empirical violation rates of 5.11% and 1.18% against theoretical targets of 5% and 1%thereby preventing liquidity shocks during extreme downturns.

Derivative market makers and options desks trading BEL 20 index instruments should calibrate volatility surfaces using heavy-tailed asymmetric specifications to prevent the systematic underpricing of out-of-the-money put options. Incorporating fat-tailed innovation distributions ($\nu \approx 8.58$) directly corrects for option implied volatility skew and smile anomalies observed during market stress. Finally, banking supervisors and central bank regulators evaluating institutional capital adequacy reserves under Basel regulatory standards should mandate asymmetric, heavy-tailed conditional variance models for internal risk assessments. Standard Gaussian assumptions underestimate capital requirements precisely when financial stability is most threatened. Implementing asymmetric volatility architectures ensures that financial institutions maintain adequate capital buffers during systemic drawdowns, enhancing overall market resilience.

Authors' Contributions:

The authors contributed equally to this work.

References:

- Almutawa, S., Hassan, H., Sankar, J. P. (2025). Stock Market Returns and Crude Oil Price Volatility: A Comparative Study Between Oil-Exporting and Oil-Importing Countries. *Journal of Risk and Financial Management*, 18(12), 713. <https://doi.org/10.3390/jrfm18120713>.
- Bai G., V., Frank, D., Birau, R., Popescu, V., B. S., M. (2024). Market volatility in cryptocurrencies: A comparative study using GARCH and TGARCH models. *Multidisciplinary Science Journal*, 7(1), 2025029. <https://doi.org/10.31893/multirev.2025029>.

**Asymmetric Volatility Dynamics and Out-of-Sample Forecasting in European Equity
Benchmarks: Evidence Analysis from a 30-Year period of BEL 20 index from stock market in
Belgium**

- Będowska-Sójka, B., Echaust, K. (2019). Commonality in Liquidity Indices: The Emerging European Stock Markets. *Systems*, MDPI journal, 7(2), 24. <https://doi.org/10.3390/systems7020024>.
- Bhowmik, R., Wang, S. (2020). Stock Market Volatility and Return Analysis: A Systematic Literature Review. *Entropy*, 22(5), 522, <https://doi.org/10.3390/e22050522>.
- Coker-Farrell, E., Imran, Z.A., Spulbar, C., Ejaz, A., Birau, R., Criveanu, R.C. (2021) Forecasting the conditional heteroscedasticity of stock returns using asymmetric models based on empirical evidence from Eastern European countries: Will there be an impact on other industries?, In: *Industria Textila*, 72, 3, 324–330, <http://doi.org/10.35530/IT.072.03.202042>.
- Duttilo, P., Gattone, S. A., Di Battista, T. (2021). Volatility Modeling: An Overview of Equity Markets in the Euro Area during COVID-19 Pandemic. *Mathematics*, 9(11), 1212. <https://doi.org/10.3390/math9111212>.
- Meher, B.K., Puntambekar, G.L., Birau, R., Hawaldar, I.T., Spulbar, C., Simion, M.L. (2023) Comparative Investment decisions in emerging textile and FinTech industries in India using GARCH models with high-frequency data, In: *Industria Textila*, 74, 6, 741–752, <http://doi.org/10.35530/IT.074.06.202311>.
- Mhadhbi, K., & Ghanmi, Y. (2025). Volatility Transmission Between European Stock Indices and the Tunisian TUNINDEX: A GARCH-BEKK Approach. *Computer Sciences & Mathematics Forum*, 11(1), 36. <https://doi.org/10.3390/cmsf2025011036>.
- Pourmansouri, R., Birau, R., (2024) *Financial Econometrics*, Cambridge Scholars Publishing, UK, ISBN: 1-0364-1034-X, ISBN13: 978-1-0364-1034-6, pp. 392, <https://www.cambridgescholars.com/product/978-1-0364-1034-6>.
- Raza, S., Shreevastava, A., Kumar Meher, B., Birau, R., Anand, A., Kumar, S., Simion, M.L., Cirjan, N.T. (2024). Predictive Analysis of Volatility for BSE S&P GREENEX index using GARCH Family Models: A case study for Indian stock market. *Revista de Științe Politice. Revue des Sciences Politiques*, no. 84, pp. 54 – 67.
- Trivedi, J., Afjal, M., Spulbar, C., Birau, R., Inumula, K.M., Mitu, N.E. (2022) Investigating the impact of COVID-19 pandemic on volatility patterns and its global implication for textile industry: An empirical case study for Shanghai Stock Exchange of China, In: *Industria Textila*, 73, 4, 365–376, <http://doi.org/10.35530/IT.073.04.202148>.

Article Info

Received: August 21 2026

Accepted: September 04 2026

How to cite this article:

Shreevastava, A., Meher, B.K., Birau, R., Popescu, V., Lupu (Filip), G. A. M., Nioata (Chireac), R. -M. (2026). Asymmetric Volatility Dynamics and Out-of-Sample Forecasting in European Equity Benchmarks: Evidence Analysis from a 30-Year period of BEL 20 index from stock market in Belgium. *Revista de Științe Politice. Revue des Sciences Politiques*, no. 91, pp. 202-216.